**UNDERGRADUATE TEXTS The** Sally **SERIES**Pure and Applied **5** 

Advanced

Calculus

Second Edition

**Patrick M. Fitzpatrick**

American Mathematical Society

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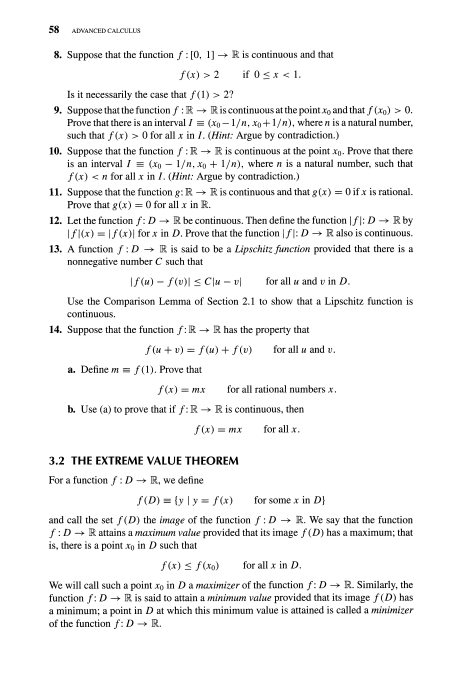
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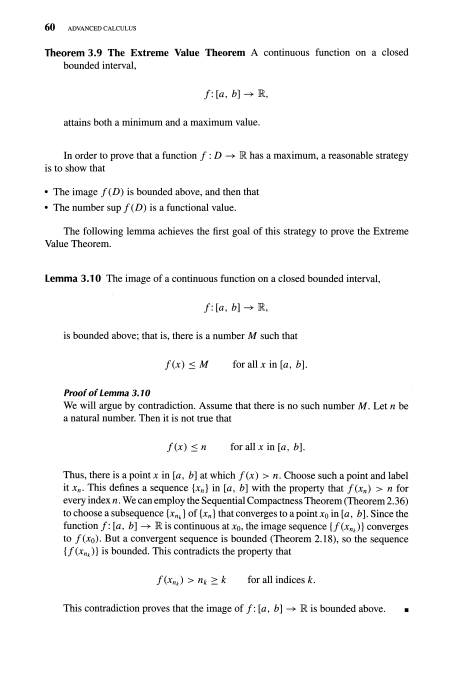
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